

Emissions, earthquakes, economics: Benefits of super fracking questioned

The piece "Super fracking" by Donald Turcotte, Eldridge Moores, and John Rundle (PHYSICS TODAY, August 2014, page 34) was quite informative.

The authors state that "carbon dioxide emissions from power plants have been reduced by about a factor of two." That may be true if one only takes the US into consideration, but it does not account for the displacement of US coal production to Europe,¹ where it is now a low-cost fuel that is producing, one imagines, a similar amount of CO₂ as it did in the US.

Another statement that requires some caution concerns the likelihood of an earthquake occurring during hydraulic fracturing. The authors suggest that the probability of a magnitude 4 earthquake is extremely low. Although, again, that may be true, the analysis does not cover water-disposal activity: The effects of long-term pressure buildup in disposal wells can produce earthquakes of greater magnitude than hydraulic fracking per se. One such quake in Oklahoma was reported² at magnitude 5.6.

The authors then state that fracking is a "successful tool for *economically* extracting oil and gas" (my italics). That is quite a bold claim and one that in the US is quite contentious, at least for gas production. Witness the 2012 remark from ExxonMobil CEO Rex Tillerson that the company and others were "losing our shirts" on shale gas.³

References

1. G. Chazan, G. Wiesmann, "Shale gas boom sparks EU coal revival," *Financial Times*, 3 February 2013.
2. StateImpact Oklahoma, "Exploring the Link Between Earthquakes and Oil and

Gas Disposal Wells," <http://stateimpact.npr.org/oklahoma/tag/earthquakes>.

3. J. A. Dicolo, T. Fowler, "Exxon: 'Losing our shirts' on natural gas," *Wall Street Journal*, 27 June 2012.

Neil McNaughton
(info@oilit.com)
Oil IT Journal
The Data Room
Sèvres, France

A building's effect on gravity experiments

Amidst the descriptions by Clive Speake and Terry Quinn ("The search for Newton's constant," PHYSICS TODAY, July 2014, page 27) of eliminating effects of the planet's pull and handling a plethora of electronic and mechanical problems in order to measure gravity, one issue seems missing: the effects of the mass of the building in which the experiments were performed. Buildings are massive compared with the test and source masses, and the distances from walls and ceilings are small enough to make their effects noticeable in, say, the fourth decimal place of the measurement. Wouldn't you need to use a massive spherical chamber devoid of other mass so that the effects would cancel each other?

Perhaps I've misunderstood or failed to notice any discussion of this in the article. Could the experiments be done outdoors above a flat plain with no mountains or buildings within miles? The problem seems way too simple a thing to have been overlooked by so many diligent people; perhaps it was considered and compensation made. I would be interested in how, if the authors could take time to explain.

J. W. Lane
(benlon@yahoo.com)
Tallahassee, Florida

■ **Speake and Quinn reply:** The effects of local gravity gradients in *G* experiments are almost always negligible because the experiments are designed so that only changes in the gravity gradients that are in phase with the experiment's sequence of operations would have any effect. Thus, unless the lab walls, nearby elevators, heavy vehicles,

or any other large mass is moving in phase with the experiment, there will be no effect. Changes that aren't precisely in phase with the experiment would increase gravitational noise but would not alter the measured signal. (Because our torsion balance was carefully designed, even that gravitational noise falls off as the fifth power of the distance.)

There could be an effect, however, if the source masses—the repositionable masses that couple with the smaller, test masses on a torsion balance or pendulum—were sufficiently large to move the torsion balance or pendulum enough to place it in a significantly different part of the local background gravitational field. In laboratory-sized experiments, however, the movements in torsion balances and pendulums are many orders of magnitude below the level at which such effects could be significant. In our experiment, for example, the rotation of the torsion balance was, at most, only some 150 microradians, with the test masses on the balance moving only about 15 micrometers. The change in local gravity field over that distance is negligible.

Clive Speake
University of Birmingham
Birmingham, UK
Terry Quinn
(tjqfrs@gmail.com)
International Bureau of Weights and Measures
Sèvres, France

Schrödinger's radial equation

The August 2014 issue of PHYSICS TODAY contains a letter (page 8) in which M. Y. Amusia comments on the article "Bohr's molecular model, a century later" by Anatoly Svidzinsky, Marlan Scully, and Dudley Herschbach (PHYSICS TODAY, January 2014, page 33). Amusia points out that the radial part of the article's *D*-dimensional Schrödinger equation in Hartree units is

$$\left\{ -\frac{1}{2} \frac{\partial^2}{\partial r^2} + \frac{[l + (D-3)/2][l + (D-1)/2]}{2r^2} - \frac{Z}{r} \right\} \phi = E\phi,$$

and he criticizes the implication that the Coulomb potential does not depend on *D*, which it surely does. Half a century

Letters and commentary are encouraged and should be sent by email to ptletters@aip.org (using your surname as the Subject line), or by standard mail to Letters, PHYSICS TODAY, American Center for Physics, One Physics Ellipse, College Park, MD 20740-3842. Please include your name, work affiliation, mailing address, email address, and daytime phone number on your letter and attachments. You can also contact us online at <http://contact.physicstoday.org>. We reserve the right to edit submissions.

Saint-Saëns scores bell-like piano tones

Here's a brief addendum to the Readers' Forum item (PHYSICS TODAY, October 2014, page 10) regarding bell tones from the piano. The unknown piece of music mentioned by Jon Orloff in his exchange with Murray Campbell about such bell tones might well be Piano Concerto no. 5, sometimes called the *Egyptian Concerto*, by Camille Saint-Saëns—specifically the second movement, a small portion of which is shown below. The bell-like quality of the sound that comes from the piano is an artifact of the way Saint-Saëns

scored the piano part. The left hand plays a series of notes moderately loud (*mf*), which the listener hears as the melody. Simultaneously, the right hand plays the twelfth above each lower note, and the sixth above that, very softly (*pp*). Those two notes are harmonics (3:1 and 5:1, respectively) of the lower note, and when they are played together with it, they blend with the lower note and give it an exotic, bell-like timbre.

Myron Levitsky
(gipsyfiddle@earthlink.net)
New York City



ago, following up on the work of Paul Ehrenfest,¹ who had studied the hydrogen atom in n spatial dimensions using Bohr orbit theory, I reformulated the problem² using Schrödinger's equation extended to n dimensions, in which I had the Coulomb potential for $n \geq 3$. I did not include the Coulomb potential for $n = 1, 2$, as discussed by Amusia, as I was only interested in the stability of the higher-dimensional atom for $n > 3$. (For the dimensionality of space I used " n " rather than " D .") In that work I gave the radial equation equivalent to the one above: I wrote, "If we now transform to n -dimensional polar coordinates, introduce n -dimensional spherical harmonics, and factor out the angular dependence,³ the resulting radial equation takes the form

$$\frac{d^2}{dr^2} + \frac{n-1}{r} \frac{dR}{dr} + \frac{2m}{\hbar^2} \left[E - \frac{\hbar^2 l(l+n-2)}{2m r^2} + \frac{e^2}{(n-2)r^{n-2}} \right] R = 0$$

In my paper, I did not eliminate the dR/dr term to arrive at a form equivalent to the first equation. However, that is readily done by setting $R = r^{-(n-1)/2} \phi$ and generalizing to nuclear charge Z , and setting $n \rightarrow D$. The reason I have the D -

dependent Coulomb potential for $D > 3$ and the article authors do not is that they have a different goal—to gain new insight into the real, atomic-molecular 3D world using the limiting behavior of the D -dimensional kinetic energy. In contrast, as indicated above, I was only interested in whether the D -dimensional Schrödinger "hydrogen atom" would have stable bound states for $D > 3$.

References

1. P. Ehrenfest, *Proc. Amsterdam Acad.* **20**, 200 (1917); *Ann. Phys. Leipzig* **61**, 440 (1920).
2. F. R. Tangherlini, *Nuovo Cimento* **27**, 636 (1963).
3. See, for example, A. Sommerfeld, *Partial Differential Equations in Physics*, E. G. Straus, trans., Academic Press (1949), app. 4.

Frank R. Tangherlini
(frtan96@gmail.com)
San Diego, California

Modeling Maxwell's Demon

The interesting article "Engineering Maxwell's demon" by Zhiyue Lu, Dibyendu Mandal, and Christopher Jarzynski in the August 2014 issue (page 60) includes a link to a video, created using the three-dimensional ani-

mation software Blender, of the device. I've used GlowScript to make an interactive version at http://www.glowscript.org/#/user/Bruce_Sherwood/folder/Pub/program/MaxwellDemon.

The program lets the user zoom and rotate to inspect the device, and it plots the demon's rotational velocity component as a function of time. The plot demonstrates the counterclockwise bias over long times that the authors describe. A user can observe the increased informational entropy in the paddle positions. A modern browser that supports the 3D graphics library WebGL and a graphics card with graphics processing units are required; click "Help" in the upper right corner for details on system requirements. Click "Edit this program" to see the code, which is short for a program of this complexity. I thank the article's authors for helpful advice.

Bruce Sherwood
(bruce_sherwood@ncsu.edu)
Santa Fe, New Mexico

Corrections

February 2015, page 45—The Osirak reactor was in Iraq.

February 2015, page 50—The late heavy bombardment period occurred 4 billion years ago. ■



adelphi
TECHNOLOGY, INC.

Neutron Generators

- Fast and thermal neutrons!
- Great for Neutron Activation Analysis
- Moderator & shielding available
- Easily operated and serviced

DD109
6 x 10⁹ Fast n/s



Like having your own personal nuclear reactor!

DD110MB
2 x 10¹⁰ Fast n/s
5 x 10⁷ Thermal n/s/cm²



www.adelphitech.com
Adelphi Technology Inc., 2003 East Bayshore Road
Redwood City, CA 94063, USA
info@adelphitech.com, +1 650-474-2750