

SUPERHEAVY COSMIC-RAY trajectory is recorded in 1/4-mm-thick sheet of Lexan plastic that was etched in sodium-hydroxide solution, which attacks plastic more rapidly along path of heavily ionizing particle than elsewhere. This side view shows nucleus entering at base of one cone and leaving at other (*Phys. Rev. Letters* 21, 630, 1968). The four photos were taken by varying the focus of microscope.

for neutron-rich fission products coming from $_{110}\mathrm{X}^{294}.$

P. H. Fowler of the University of Bristol and his collaborators have been scanning the skies at high altitudes with a detector consisting of iron sheets sandwiched between nuclear emulsions. They have reported evidence for elements up to uranium in cosmis rays (*Proc. Roy. Soc.* A301, 39, 1967) and more recently for one particle they believe may be heavier than uranium.

Using huge detector arrays of interleaved plastic track detectors and nuclear emulsions, groups at General Electric (Robert L. Fleischer, P. Buford Price and Glenn E. Nichols) and Washington University (George Blanford, Michael W. Friedlander, Joseph Klarmann, Robert M. Walker, John Wefel and William Wells) have found several nuclei about as heavy as those found by the Bristol team and have established that the nuclei were recorded at ceiling altitude (37 km) and were truly relativistic. Following three recent balloon flights with Fowler's group they have located the tracks of about 40 relativistic superheavy nuclei that they traced through the plastics and emulsions. All three groups are proceeding with the rigorous identification of these nuclei, some of which may be heavier than uranium. —CBL

Mind Your k's and q's to Simplify Solid-State Theory

Many solid-state theorists are enthused about a new quantum-mechanical representation recently developed by Joshua Zak of the Technion, Haifa (while at the Bitter National Magnet Laboratory, MIT). Zak's "kq representation" can be used to reproduce in an almost trivial way the many earlier and often complicated derivations of electron behavior in a periodic potential.

Although the uncertainty principle prevents treating particle coördinate x and momentum p together, in some situations precise information about either the coördinate or the momentum is irrelevant, Zak explains. In a solid where the potential is periodic, all the unit cells are identical; so all you need specify is the position of a particle within any such cell. He uses the well-known solid-state concept of quasi-momentum (reduced wave vector) defined so that exp (−ik•t) is the eigenvalue of the operation of translation by the lattice vector \mathbf{t} in ordinary space; p can equal k, $k + 2\pi/a$, $k + 2(2\pi/a)$, etc. Similarly he specifies the position by a quasi-coördinate q, which ranges only over the volume of a unit cell and is defined so that $\exp(i\mathbf{K}\cdot\mathbf{q})$ is the eigenvalue of the operation of translation by the reciprocal lattice vector \mathbf{K} in momentum space. k and q can be measured together, and they form the kq representation. Zak emphasizes that the uncertainty principle is not violated by the representation, since one only uses partial information about the coördinates.

Zak has applied his kq representation to the motion of electrons in solids in external fields. The derivation of the acceleration theorem for a Bloch electron in an electric field, $\hbar k = -eE$ usually involves quite complicated expansions and integrations, Zak notes. But with his representation k is an independent variable in Schrödinger's equation, and the theorem follows at once from the simple quantum-mechanical rule that the time variation of k is given by the commutator of the Hamiltonian with k.

For a Bloch electron in a magnetic field, the main result of the effective Hamiltonian follows at once from Schrödinger's equation in the kq representation.

Zak is presently at Northwestern University.

New Insight Is Offered into the Fission Process

The existence of a double-humped fission barrier appears to be the explanation for the behavior of a wide range of heavy and superheavy nuclei.

This type of fission behavior was predicted by V. Strutinski1 of the Kurchatov Institute (on leave at the Niels Bohr Institute), who calculated shellenergy corrections to the liquid-drop model as a function of deformation. These corrections modify the singlehumped fission barier obtained previously with the uncorrected liquiddrop model to produce two humps (or more) separated by a well (figure 1). This well appears for rather large deformations ($\beta = 0.5$ to 0.6, where high values for β mean great deformation). The well allows formation of intermediate quasi-stationary states of the compound nucleus at these deformations.

The ground state, corresponding to the bottom of the second well, can explain the existence of spontaneously fissioning isomers, first observed by S. M. Polikanov and G. N. Flerov (Joint Institute for Nuclear Studies, Dubna) about seven years ago.

Saclay studies.² The excited states in the well can be responsible for certain structure effects found in some fission cross sections. The most spectacular of these effects is the intermediate structure in the cross section for subthreshold fission induced by resonance neutrons. Such structure was first observed and reported in 1966 by André Michaudon, Jacques Blons, A. Fubini and D. Paya at Saclay, in the fission cross section of Np²³⁷; the 45-MeV electron linac served as a pulsed neutron source. Since at that time such intermediate structure was