

ENERGY PRODUCTION IN STARS

"... stars have a life cycle much like animals. They get born, they grow, they go through a definite internal development, and finally they die . . ."

HANS A. BETHE

FROM TIME IMMEMORIAL people must have been curious to know what keeps the sun shining. The first scientific attempt at an explanation was by Helmholtz about one hundred years ago, and was based on the force most familiar to physicists at the time, gravitation. When a gram of matter falls to the sun's surface it gets a potential energy

$$E_{\text{pot}} = -GM/R = -1.91 \times 10^{15} \text{ erg/gm} \quad (1)$$

where $M = 1.99 \times 10^{33}$ gm is the sun's mass, $R = 6.96 \times 10^{10}$ cm its radius, and $G = 6.67 \times 10^{-8}$ the gravitational constant. A similar energy was set free when the sun was assembled from interstellar gas or dust in the dim past; actually somewhat more, because most of the sun's material is located closer to its center, and therefore has a numerically larger potential energy. One-half of the energy set free is transformed into kinetic energy according to the well-known virial theorem of mechanics. This will permit us later to estimate the temperature in the sun. The other half of the potential energy is radiated away. We know that at present the sun radiates

$$\epsilon = 1.96 \text{ erg/gm sec} \quad (2)$$

Therefore, if gravitation supplies the energy, there is enough energy available to supply the radiation for about 10^{15} sec which is about 30 million years.

This was long enough for nineteenth-century physicists, and certainly a great deal longer than man's recorded history. It was not long enough for the biologists of the time. Darwin's theory of evolution had just become popular, and biologists argued with Helmholtz that evolution would require a longer time than 30 million years, and that therefore his energy source for the sun was insufficient. They were right.

At the end of the 19th century, radioactivity was discovered by Becquerel and the two Curies who received

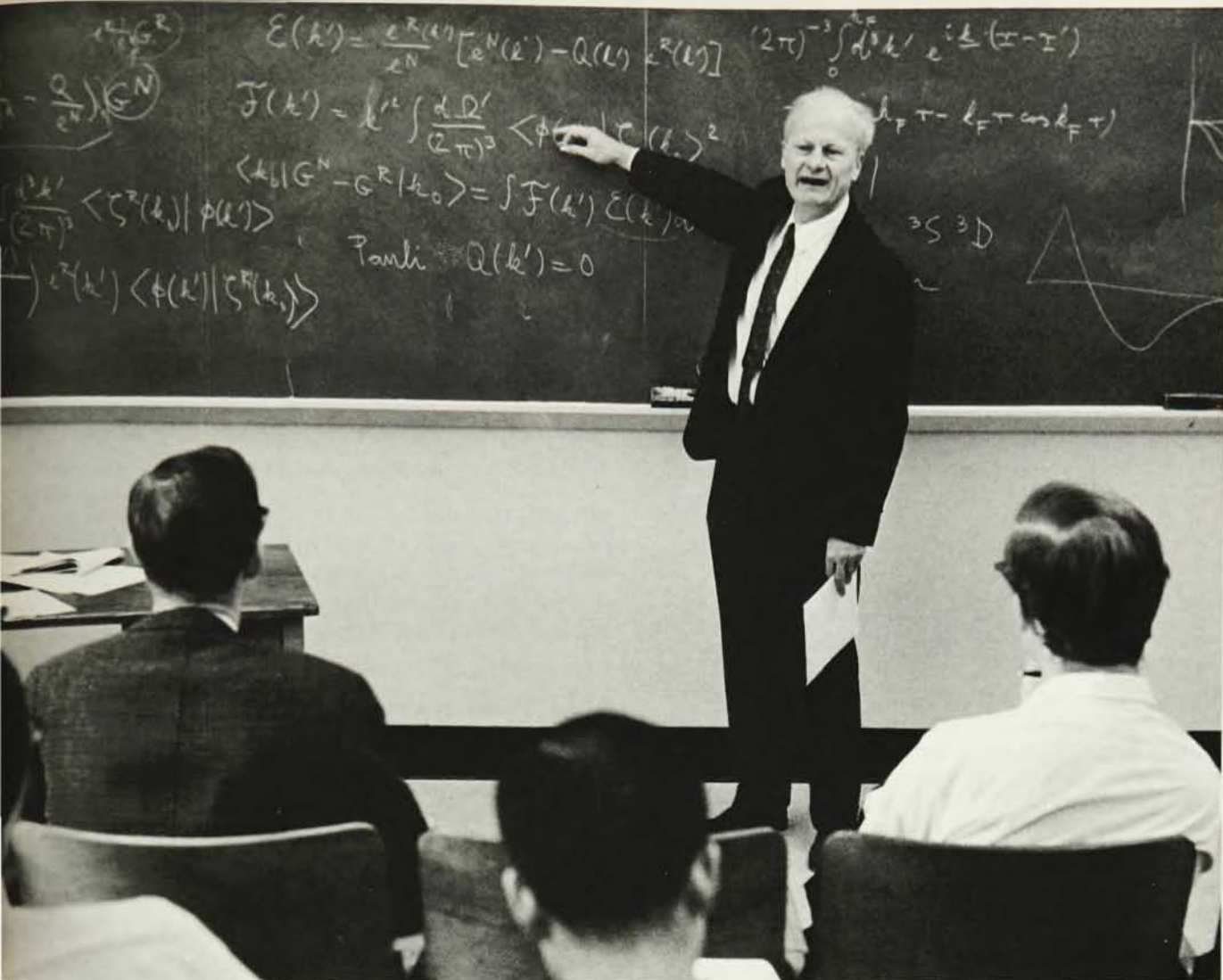
one of the first Nobel prizes for this discovery. Radioactivity permitted a determination of the age of the earth, and more recently, of meteorites which indicate the time at which matter in the solar system solidified. On the basis of such measurements the age of the sun is estimated to be 5 milliards of years, within about 10% [1 milliard = 10^9]. So gravitation is not sufficient to supply its energy over the ages.

Eddington, in the 1920's, investigated very thoroughly the interior constitution of the sun and other stars, and was much concerned about the sources of stellar energy. His favorite hypothesis was the complete annihilation of matter, changing nuclei and electrons into radiation. The energy which was to be set free by such a process, if it could occur, is given by the Einstein relation between mass and energy and is

$$c^2 = 9 \times 10^{20} \text{ erg/gm} \quad (3)$$

This would be enough to supply the sun's radiation for 1500 milliards of years. However, nobody has ever observed the complete annihilation of matter. From experiments on earth we know that protons and electrons do not annihilate each other in 10^{30} years. It is hard to believe that the situation would be different at a temperature of some 10 million degrees such as prevails in the stars, and Eddington appreciated this difficulty quite well.

From the early 1930's it was generally assumed that the stellar energy is produced by nuclear reactions. Already in 1929, Atkinson and Houtermans¹ concluded that at the high temperatures in the interior of a star, the nuclei in the star could penetrate into other nuclei and cause nuclear reactions, releasing energy. In 1933, particle accelerators began to operate in which such nuclear reactions were actually observed. They were found to obey very closely the theory of Gamow, Condon and Gurney, on the penetration of charged par-



Hans A. Bethe received the 1967 Nobel Prize in physics for "his contributions to the theory of nuclear reactions, especially his discoveries concerning energy production of stars." He obtained his doctorate from the University of Munich in 1928, worked at Frankfurt, Stuttgart, Munich, Cambridge (with Rutherford) and Rome (with Fermi). In 1935 he joined the staff of Cornell University, where he is

still. During World War II he was head of the theoretical-physics division at Los Alamos Scientific Laboratory. In this article, his Nobel Prize acceptance speech, he outlines the work on nuclear reactions in stars for which the Prize was awarded; other important work has included that on the stopping power of matter for fast particles and on the theory of pair formation in the electric field of a nucleus.

ticles through potential barriers. In early 1938, Gamow and Teller² revised the theory of Atkinson and Houtermans on the rate of "thermonuclear" reactions, ie nuclear reactions occurring at high temperature. At the same time, Weizsäcker³ speculated on the reactions which actually might take place in the stars.

In April 1938, Gamow assembled a small conference of physicists and astrophysicists in Washington, D.C. This conference was sponsored by the Department of Terrestrial Magnetism of the Carnegie Institution. At this Conference, the astrophysicists told us physicists what they knew about the internal constitution of the stars. This was quite a lot, and all their results had been derived without knowledge of the specific source of energy. The only assumption they made was that most of the energy was produced "near" the center of the star.

Properties of stars

The most easily observable properties of a star are its total luminosity and its surface temperature. In rela-

tively few cases of nearby stars, the mass of the star can also be determined.

Figure 1 shows the customary Hertzsprung-Russell diagram. The luminosity, expressed in terms of that of the sun, is plotted against the surface temperature, both on a logarithmic scale. Conspicuous is the main sequence, going from upper left to lower right, ie from hot and luminous stars to cool and faint ones. Most stars lie on this sequence. In the upper right are the red giants, cool but brilliant stars. In the lower left are the white dwarfs, hot but faint. We shall be mainly concerned with the main sequence. After being assembled by gravitation, stars spend the most part of their life on the main sequence, then develop into red giants, and in the end, probably into white dwarfs. The figure shows that typical surface temperatures are of the order of 10^4K .

Figure 2 gives the relation between mass and luminosity in the main sequence. At the upper end, beyond about 15 sun masses, the mass determinations are uncertain. It is clear, however, that luminosity in-

creases rapidly with mass. For a factor of 10 in mass, the luminosity increases by a factor of about 3000, hence the energy production per gram is about 300 times larger.

To obtain information on the interior constitution of the stars, astrophysicists integrate two fundamental equations. Pioneers in this work have been Eddington, Chandrasekhar and Strömberg. The first equation is that of hydrostatic equilibrium

$$\frac{dP}{dr} = -GM(r) \frac{\rho(r)}{r^2} \quad (4)$$

in which P is the pressure at distance r from the center, ρ is the density and $M(r)$ is the total mass inside r . The second equation is that of radiation transport

$$\frac{1}{\chi \rho} \frac{d}{dr} \left(\frac{1}{3} ac T^4 \right) = -\frac{L(r)}{4\pi r^2} \quad (5)$$

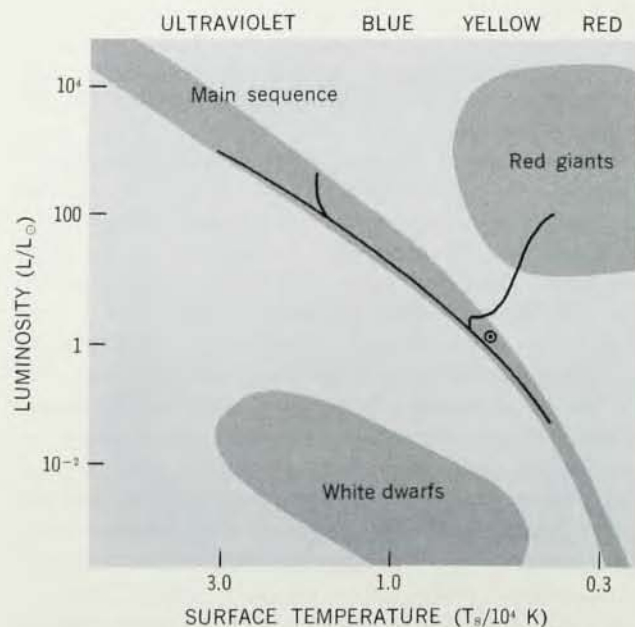
Here χ is the opacity of the stellar material for black-body radiation of the local temperature T , a is the Stefan-Boltzmann constant, and $L(r)$ is the flux of radiation at r . The value of L at the surface R of the star is the luminosity. In the stars we shall discuss, the gas obeys the equation of state

$$P = RT \rho / \mu \quad (6)$$

where R is the gas constant, while μ is the mean molecular weight of the stellar material. If X , Y and Z are respectively concentrations by mass of hydrogen, helium and all heavier elements, and if all gases are fully ionized, then

$$\mu^{-1} = 2X + 3Y/4 + Z/2 \quad (7)$$

In all stars except the very oldest ones, it is believed that Z is between 0.02 and 0.04; in the sun at present, X is about 0.65, hence, $Y = 0.33$ and $\mu = 0.65$. In many stars the chemical composition, especially X and Y , vary with position r . The opacity is a complicated function



HERTZSPRUNG-RUSSELL DIAGRAM. From E. E. Salpeter, in *Apollo and the Universe*, Science Foundation for Physics, University of Sydney, Australia (1967). —FIG. 1

of Z and T , but in many cases it behaves like

$$\chi = C \rho T^{-3.5} \quad (8)$$

where C is a constant.

The integration of (4) and (5) in general requires computers. However an estimate of the central temperature may be made from the virial theorem which we mentioned in the beginning. According to this, the average thermal energy per unit mass of the star is one-half of the average potential energy. This leads to the estimate of the thermal energy per particle at the center of the star

$$kT_c = \alpha \mu GHM/R \quad (9)$$

in which H is the mass of the hydrogen atom, and α is a constant whose magnitude depends on the specific model of the star but is usually about 1 for main sequence stars. Using this value, and (1), we find for the central temperature of the sun

$$T_{6c} = 14 \quad (10)$$

where T_6 denotes the temperature in millions of degrees, here and in the following. A more careful integration of the equations of equilibrium by Demarque and Percy⁴ gives

$$T_{6c} = 15.7; \rho_c = 158 \text{ gm/cm}^3 \quad (11)$$

Originally Eddington had assumed that the stars contain mainly heavy elements, from carbon on up. In this case $\mu = 2$ and the central temperature is increased by a factor of 3, to about 40 million degrees; this led to contradictions with the equation of radiation flow, (5), if the theoretical value of the opacity was used. Strömberg pointed out that these contradictions can be resolved by assuming the star to consist mainly of hydrogen, which is also in agreement with stellar spectra. In modern calculations the three quantities X , Y , Z , indicating the chemical composition of the star, are taken to be parameters to be fixed so as to fit all equations of stellar equilibrium.

Thermonuclear reactions

All nuclei in a normal star are positively charged. In order for them to react they must penetrate each others' Coulomb potential barrier. The wave mechanical theory of this shows that in the absence of resonances, the cross section has the form

$$\sigma(E) = \frac{S(E)}{E} \exp\left(-\sqrt{\frac{E_G}{E}}\right) \quad (12)$$

where E is the energy of the relative motion of the two colliding particles, $S(E)$ is a coefficient characteristic of the nuclear reaction involved and

$$E_G = 2M(\pi Z_0 Z_1 e^2 / \hbar)^2 = (2\pi Z_0 Z_1)^2 E_{\text{Bohr}} \quad (13)$$

Here M is the reduced mass of the two particles, Z_0 and Z_1 their charges, and E_{Bohr} is the Bohr energy for mass M and charge 1. (13) can be evaluated to give

$$E_G = 0.979 W \text{ MeV} \quad (14)$$

with

$$W = AZ_0^2 Z_1^2 \quad (14 a)$$

$$A = A_0 A_1 / (A_0 + A_1) \quad (14 b)$$

in which A_0, A_1 are the atomic weights of the two colliding particles. For most nuclear reactions $S(E)$ is between 10 MeV barns and 1 keV barn.

The gas at a given r in the star has a given temperature so that the particles have a Boltzmann energy distribution. The rate of nuclear reactions is then proportional to

$$(8/\pi M)^{1/2} (kT)^{-3/2} \int \sigma(E) E \exp(-E/kT) dE \quad (15)$$

It is most convenient⁵ to write for the rate of disappearance of one of the reactants

$$dX_0/dt = -[01] X_0 X_1 \quad (16)$$

where X_0 and X_1 are the concentrations of the reactants by mass, and

$$[01] = 7.8 \times 10^{11} (Z_0 Z_1 / A)^{1/3} S_{eff} T_6^{-2/3} e^{-\tau} \quad (17)$$

$$\tau = 42.487 (W/T_6)^{1/3} \quad (17a)$$

Since the reaction cross section (12) increases rapidly with energy, the main contribution to the reaction comes from particles which have an energy many times the average thermal energy. Indeed the most important energy is

$$E_0 = (\tau/3) kT \quad (18)$$

For $T = 13$, which is an average for the interior of the sun, we have

$$\begin{aligned} \tau/3 &= 4.7 \text{ for the reaction } H + H \\ &19 \text{ for the reaction } C + H \\ &25 \text{ for the reaction } N + H \end{aligned} \quad (19)$$

It is also easy to see from (17) that the temperature dependence of the reaction rate is

$$\frac{d \log [01]}{d \log T} = \frac{\tau - 2}{3} \quad (20)$$

Nuclear reactions in main sequence stars

Evidently, at a given temperature and under otherwise equal conditions, the reactions which can occur most easily are those which have the smallest possible value of W , (14 a). This means that at least one of the interacting nuclei should be a proton, $A_0 = Z_0 = 1$. Thus we may examine the reactions involving protons.

The simplest of all possible reactions is

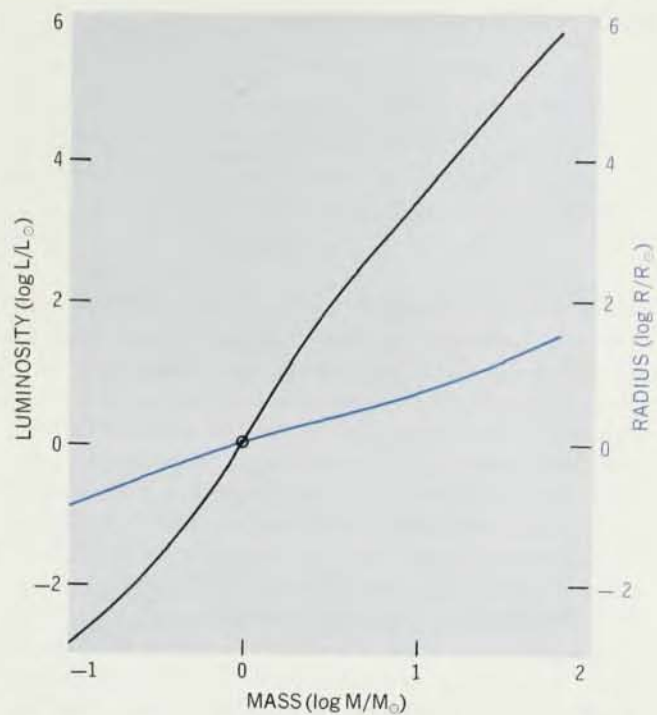


(ϵ^+ = positron, ν = neutrino).

This was first suggested by Weizsäcker³, and calculated by Critchfield and Bethe.⁶ The reaction is of course exceedingly slow because it involves the beta disintegration. Indeed the characteristic factor S is

$$S(E) = 3.36 \times 10^{-26} \text{ MeV barns} \quad (22)$$

This has been derived on purely theoretical grounds, using the known coupling constant of beta disintegration; the value is believed to be accurate to 5% or better. There is no chance of observing such a slow reaction on earth, but in the stars we have almost unlimited time, and a large supply of protons of high energy. As we shall see presently, the rate of energy production by this simple reaction fits the observed energy production in the sun very well.



LUMINOSITY AND RADIUS of stars vs mass. Abscissa is $\log M/M_\odot$. Data from C. W. Allen, *Astrophysical Quantities* (Athlone Press, 1963), p. 203. The curve for $\log L/L_\odot$ holds for all stars, that for $R/R_\odot$ only for the stars in the main sequence. The symbol $\odot$ refers to the sun. —FIG. 2

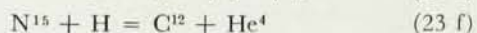
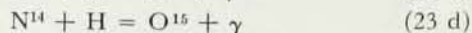
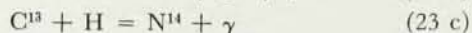
The deuterons formed in (21) will quickly react further, and the end product is He^4 . We shall discuss the reactions in more detail later on.

The proton-proton reaction (21), although it predicts the correct energy production in the sun, has a rather weak dependence on temperature. According to (19), (20), it behaves about as T^4 . Since central temperatures change only little from the sun to more massive stars, the energy production by this reaction does likewise. However as we have seen in figure 2, the observed energy production increases dramatically with increasing mass. Therefore there must exist nuclear reactions which are more strongly dependent on temperature; these must involve heavier nuclei.

Stimulated by the Washington Conference of April 1938, and following the argument just mentioned, I examined⁷ the reactions between protons and other nuclei, going up in the periodic system. Reactions between H and He^4 lead nowhere, there being no stable nucleus of mass 5. Reactions of H with Li, Be and B, as well as with deuterons, are all very fast at the central temperature of the sun, but just this speed of the reaction rules them out: The partner of H is very quickly used up in the process. In fact, and just because of this reason, all the elements mentioned, from deuterium to boron, are extremely rare on earth and in the stars, and can therefore not be important sources of energy.

The next element, carbon, behaves quite differently. In the first place, it is an abundant element, probably making up about 1% by mass of any newly formed star. Secondly, in a gas of stellar temperature, it under-

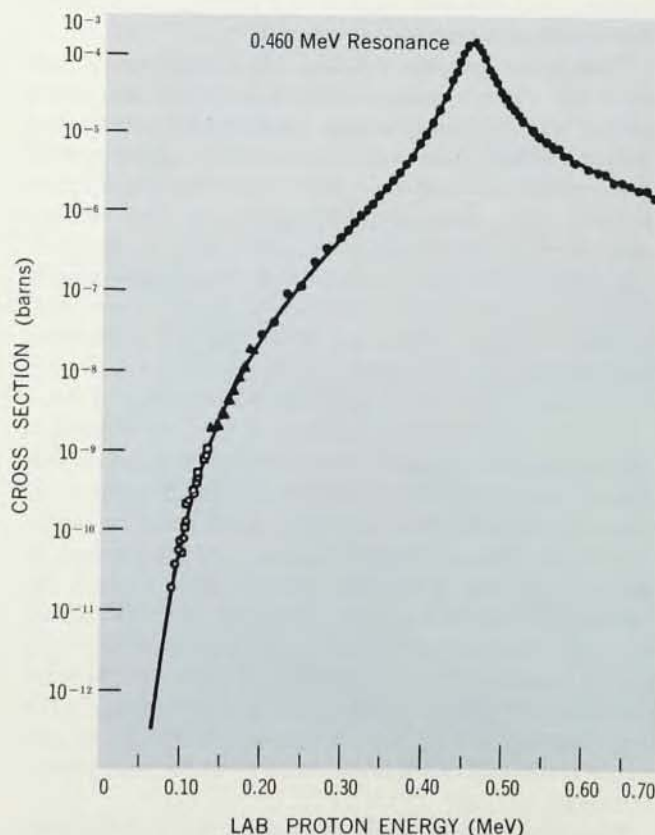
goes a cycle of reactions, as follows



Reactions a, c, and d are radiative captures; the proton is captured by the nucleus and the energy emitted in the form of gamma rays; these are then quickly converted into thermal energy of the gas. For reactions of this type, $S(E)$ is of the order of 1 keV barn. Reactions b and e are simply spontaneous beta decays, with lifetimes of 10 and 2 minutes respectively, negligible in comparison with stellar times. Reaction f is the most common type of nuclear reaction, with 2 nuclei resulting from the collision; $S(E)$ for such reactions is commonly of the order of MeV barns.

Reaction f is in a way the most interesting because it closes the cycle: We reproduce the C^{12} which we started from. In other words, carbon is only used as a catalyst; the result of the reaction is a combination of 4 protons and 2 electrons⁸ to form one He^4 nucleus. In this process two neutrinos are emitted, taking away about 2 MeV energy together. The rest of the energy, about 25 MeV per cycle, is released usefully to keep the sun warm.

Making reasonable assumptions of the reaction strength $S(E)$, on the basis of general nuclear physics,



CROSS SECTION for the reaction $\text{C}^{12} + \text{H}$, as a function of the proton energy. From Fowler, Caughlan and Zimmerman, reference 5. —FIG. 3

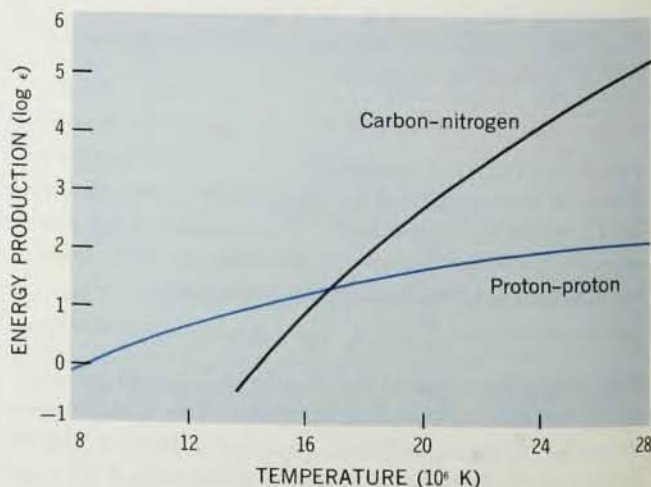
I found in 1938 that the carbon-nitrogen cycle gives about the correct energy production in the sun. Since it involves nuclei of relatively high charge, it has a strong temperature dependence, as given in (19). The reaction with N^{14} is the slowest of the cycle and therefore determines the rate of energy production; it goes about as T^{24} near solar temperature. This is amply sufficient to explain the high rate of energy production in massive stars.⁹

Experimental results

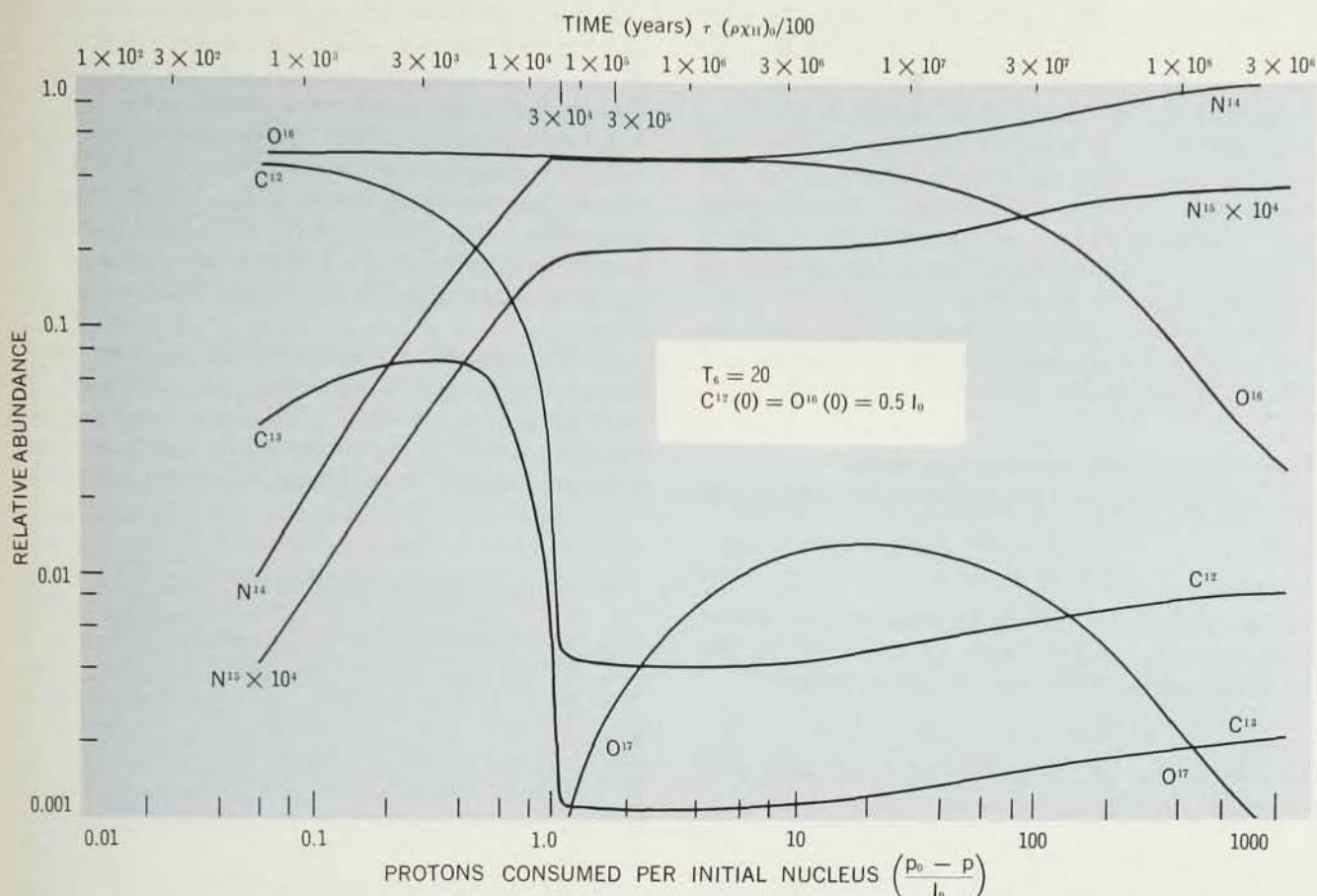
To put the theory on a firm basis, it is important to determine the strength factor $S(E)$ for each reaction by experiment. This has been done under the leadership of W. A. Fowler¹⁰ of the California Institute of Technology in a monumental series of papers extending over a quarter of a century. Not only have all the reactions in (23) been observed, but in all cases $S(E)$ has been accurately determined.

The main difficulty in this work is due to the resonances which commonly occur in nuclear reactions. Figure 3 shows the cross section of the first reaction⁵ (23 a), as a function of energy. The measured cross sections extend over a factor of 10^7 in magnitude; the smallest ones are 10^{-11} barns = 10^{-35} cm² and therefore clearly very difficult to observe. The curve shows a resonance at 460 keV. The solid curve is determined from nuclear reaction theory, on the basis of the existence of that resonance. The fit of the observed points to the calculated curve is impressive. Similar results have been obtained on the other three proton-capture reactions in (23).

On the basis of figure 3 we can confidently extrapolate the measurements to lower energy. As we mentioned in (18), the most important energy contributing to the reaction rate is about 20 kT. For $T_6 = 13$, we have $kT = 1.1$ keV; so we are most interested in the cross section around 20 keV. This is much too low an energy to observe the cross section in the laboratory; even at 100 keV, the cross section is barely observable. So quite a long extrapolation is required.



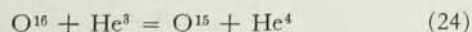
THE ENERGY PRODUCTION, in erg/gm sec, as a function of the temperature in millions of degrees, for the proton-proton reaction (P P) and the carbon-nitrogen cycle (C N). Concentrations assumed $X = Y = 0.5$, $Z = 0.02$. Calculated from Tables 8 and 9 of Reeves, reference 12. —FIG. 4



VARIATION WITH TIME of the abundances of various elements involved in the CNO cycle. It is assumed that initially C^{12} and O^{16} have the same abundance while that of N^{14} is small. From G. R. Caughlan, *Astrophys. J.* (1967). —FIG. 5

This can be done with confidence provided there are no resonances close to $E = 0$. Therefore a great deal of experimental work has gone into the search for such resonances.

The resonances exist of course in the compound nucleus, ie the nucleus obtained by adding the two initial reactants. To find resonances near the threshold of the reactions (23), it is necessary to produce the same compound nucleus from other initial nuclei, eg, in the reaction between N^{14} and H , the compound nucleus O^{15} is formed. To investigate its levels Hensley¹¹ at Cal Tech studied the reaction



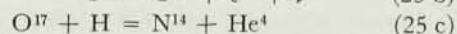
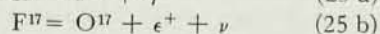
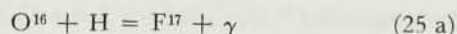
He found indeed a resonance 20 KeV below the threshold for $N^{14} + H$ which in principle might enhance the process (23 d). However the state in O^{15} was found to have a spin $J = 7/2$. Therefore, even though N^{14} has $J = 1$ and the proton has a spin of $1/2$, we need at least an orbital momentum $\lambda = 2$, to reach this resonant state in O^{15} . The cross section for such a high orbital momentum is reduced by at least a factor 10^4 , compared to $\lambda = 0$, so that the near-resonance does not in fact enhance the cross section $N^{14} + H$ appreciably. This cross section can then be calculated by theoretical extrapolation from the measured range of proton energies, and the same is true for the other reactions in the cycle (23).

On this basis, Fowler and others have calculated the

rate of reactions in the CN cycle. A convenient tabulation has been given by Reeves¹²; his results are plotted in figure 4. This figure gives the energy production per gram per second as a function of temperature. We have assumed $X = 0.5$, $Z = 0.02$. The figure shows that at low temperature the $H + H$ reaction dominates, at high temperatures the $C + N$ cycle; the crossing point is at $T_6 = 13$; here the energy production is 7 erg/gm sec. The average over the entire sun is obviously smaller, and the result is compatible with an average production of 2 erg/gm sec.

The energy production in the main sequence can thus be considered as well understood.

An additional point should be mentioned. Especially at higher temperature, when the CN cycle prevails, there is also a substantial probability for the reaction chain



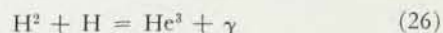
This chain is not cyclic but feeds into the CN cycle. It is customary to speak of the whole set of reactions as the CNO bi-cycle. The effect of reactions (25) is that O^{16} initially present will also contribute to the reactants available, and thus increase the reaction rate of CN cycle somewhat. This has been taken into account in figure 4.

If equilibrium is established in the CNO bi-cycle,

eventually most of the nuclei involved will end up as N^{14} because this nucleus has by far the longest lifetime against nuclear reactions. There is no observable evidence for this; in fact wherever the abundance can be observed, C and O tend to be at least as abundant as N. However this is probably due to the fact that the interior of a star stays well separated from its surface; there is very little mixing. Astrophysicists have investigated the circumstances when mixing is to be expected, and have found that surface abundances are quite compatible with these expectations. In the interstellar material which is used to form stars, we have reason to believe that C and O are abundant and N is rare. This will be discussed later.

The completion of the proton-proton chain

The initial reaction (21) is followed almost immediately by



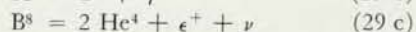
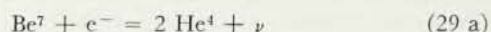
The fate of He^3 depends on the temperature. Below about $T_6 = 15$, the He^3 builds up sufficiently so that two such nuclei react with each other according to



This reaction has an unusually high $S(E) = 5$ MeV barns.⁵ At higher temperature the reaction



competes favorably with (27). The Be^7 thus formed may again react in one of two ways



At about $T_6 = 20$, reaction (29 b) begins to dominate over (29 a). (29 b) is followed by (29 c) which emits neutrinos of very high energy. Davis,¹³ at Brookhaven, is attempting to observe these neutrinos.

Evolution of a star

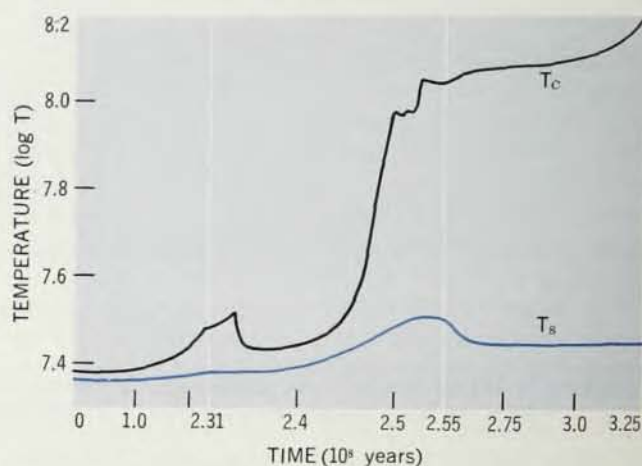
A main sequence star uses up its hydrogen preferentially near its center where nuclear reactions proceed most rapidly. After a while, the center has lost almost all its hydrogen. For stars of about twice the luminosity of the sun, this happens in less than 10^{10} years which is approximately the age of the universe, and also the age of stars in the globular clusters. We shall now discuss what happens to a star after it has used up the hydrogen at the center. Of course, in the outside regions hydrogen is still abundant.

This evolution of a star was first calculated by Schwarzschild¹⁴ who has been followed by many others; we shall use recent calculations by Iben.¹⁵ When hydrogen gets depleted, not enough energy is produced near the center to sustain the pressure of the outside layers of the star. Hence gravitation will cause the center to collapse. Thereby, higher temperatures and densities are achieved. The temperature also increases farther out where there is still hydrogen left, and this region now begins to burn. After a relatively short time, a shell of H, away from the center, produces most of the energy; this shell gradually moves outward

and gets progressively thinner as time goes on.

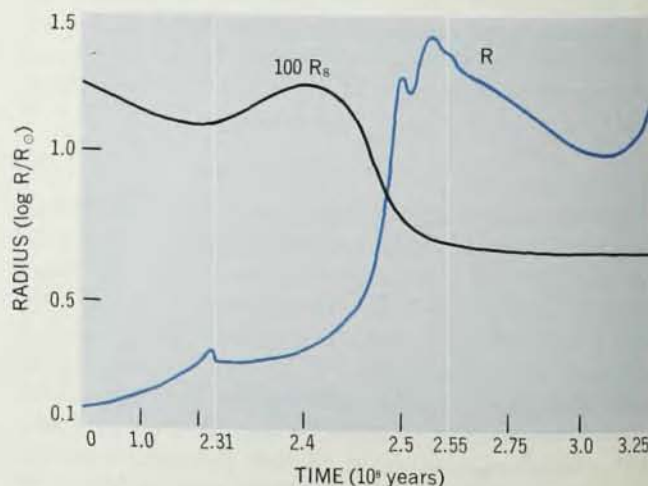
At the same time, the region of the star outside the burning shell expands. This result follows clearly from all the many numerical computations on this subject. The physical reason is not clear. One hypothesis is that it is due to the discontinuity in mean molecular weight: Inside the shell, there is mostly helium, of $\mu = 4/3$, outside we have mostly hydrogen, and $\mu = 0.65$. Another suggestion is that the flow of radiation is made difficult by the small radius of the energy source, and that this has to be compensated by lower density just outside the source.

By this expansion the star develops into a red giant. Indeed, in globular clusters (which, as I mentioned, are made up of very old stars), all the more luminous stars are red giants. In the outer portion of these stars, radiative transport is no longer sufficient to carry the



EVOLUTION OF A STAR of 3 solar masses, according to I. Iben, *Astrophys. J.* 142, 1447 (1965). Abscissa is time in units of 10^8 years (note the breaks in scale at $t = 2.31$ and 2.55). I. Temperature (on logarithmic scale): T_c = temperature at center of star, T_s = same at midpoint of source of energy generation, which after $t = 2.48$ is a thin shell. T_c increases enormously, T_s stays almost constant.

—FIG. 6



EVOLUTION OF A STAR, see caption to figure 6. II. Radius, in units of that of the sun, on logarithmic scale. R = total radius, $100 R_s$ = 100 times the radius of midpoint of energy source. R increases tremendously, while R_s shrinks somewhat.

—FIG. 7

energy flow; therefore convection of material sets in in these outer regions. This convection can occupy as much as the outer 80% of the mass of the star; it leads to intimate mixing of the material in the convection zone.

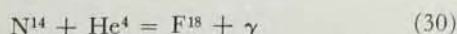
Iben¹⁵ has discussed a nice observational confirmation of this convective mixing. The star Capella is a double star, each component having a mass of about 3 solar masses, and each being a red giant. The somewhat lighter star, Capella F (its spectral type is F) shows noticeable amounts of Li in its spectrum, while the somewhat heavier Capella G shows at least 100 times less Li. It should be expected that G, being heavier, is farther advanced in its evolution. Iben now gives arguments that the deep-reaching convection and mixing which we just discussed, will occur just between the evolution phases F and G. By convection, material from the interior of the star will be carried to the surface; this material has been very hot and has therefore burned up its Li. Before deep convection sets in (in star F) the surface Li never sees high temperatures and thus is preserved.

Following the calculations of Iben we have plotted in figures 6 to 9 the development of various important quantities in the history of a star of mass = 3 solar masses. The time is in units of 10^8 years. Since the developments go at very variable speed, the time scale has been broken twice, at $t = 2.31$ and $t = 2.55$. In between is the period during which the shell source develops.

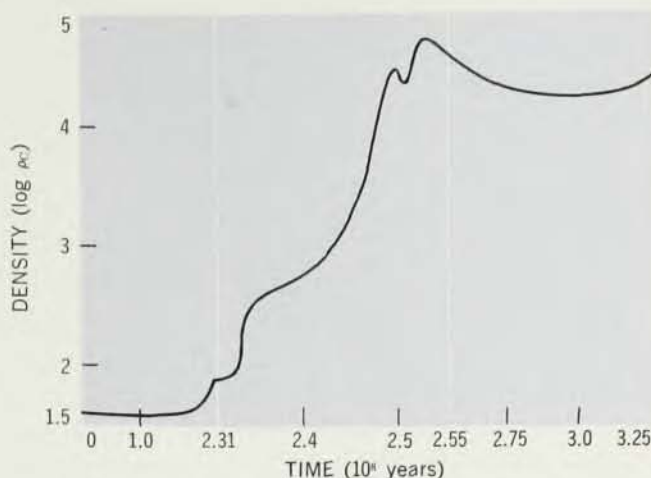
During this period the central temperature rises spectacularly (figure 6), from about $T_6 = 25$ to $T_6 = 100$. At the same time the radius increases from about 2 to 30 solar radii; subsequently, it decreases again to about 15 (figure 7). The central density, starting at about 40, increases in the same period to about 5×10^4 . The luminosity (figure 9) does not change spectacularly, staying always between 100 and 300 times that of the sun.

While the inside and the outside of the star undergo such spectacular changes, the shell in which the hydrogen is actually burning does not change very much. Figure 9 shows m , the fraction of the mass of the star enclosed by the burning shell. Even at the end of the calculation, $t = 3.25$, this is only $m = 0.2$. This means that only 20% of the hydrogen in the star has burned after all this development. Figure 6, curve T_s , shows the temperature in the burning shell which stays near 25 million degrees all the time. Figure 7, curve R_s , shows the radius of the shell, in units of the solar radius; during the critical time when the shell is formed this radius drops from about 0.15 to 0.07. This is of course the mechanism by which the shell is kept at the temperature which originally prevailed at the center.

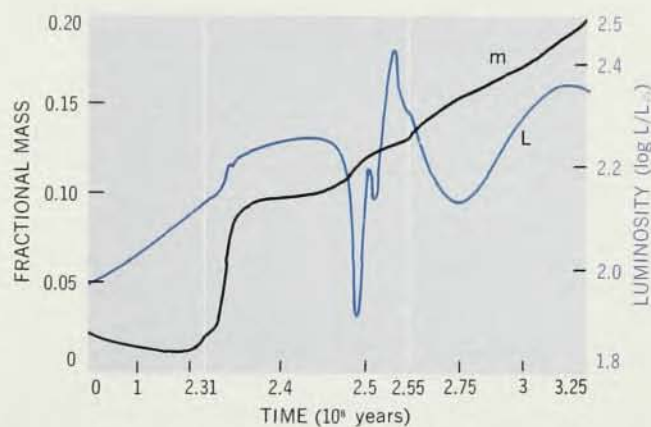
In the meantime, the temperature at the center increases steadily. When it reaches about $T_6 = 100$, the He^4 which is abundant at the center, can undergo nuclear reactions. The first of these, which occurs at the lowest temperature (about $T_6 = 90$) is



While this reaction goes on, the central temperature remains fairly constant. However, there is not much N^{14} so the reaction soon stops (after about 0.02×10^8 years),



EVOLUTION OF A STAR, see caption to figure 6. III. Density, on logarithmic scale, at the center of the star. This quantity increases about 1000-fold. —FIG. 8



EVOLUTION OF A STAR, see caption to figure 6. IV. Curve L , luminosity relative to that of the sun, on logarithmic scale. This quantity does not change very much during the life of the star. Curve m , fraction of the mass of the star enclosed by energy-producing shell, on linear scale. This fraction increases slowly with time. —FIG. 9

and the center contracts further.

The next reaction makes use entirely of the abundant He^4 , viz



This reaction has the handicap of requiring a simultaneous collision of 3 alpha particles. This would be extremely unlikely were it not for the fact that it is favored by a *double* resonance. Two alpha particles have nearly the same energy as the unstable nucleus Be^8 , and further $\text{Be}^8 + \text{He}^4$ has almost the same energy as an excited state of C^{12} . This reaction can of course not be observed in the laboratory but the two contributing resonances can be. The importance of the first resonance was first suggested by Salpeter,¹⁶ the second by Hoyle.¹⁷ Recent data indicate that (31) requires a temperature of about $T_6 = 110$, at the central densities corresponding to $t = 2.5$, ie $\rho_c > 10^4$. Once this reac-

tion sets in, the central temperature does not rise very fast any more.

Reaction (31) is most important for the buildup of elements. Early investigators^{5,7} had great trouble with bridging the gap between He^4 and C^{12} . Two nuclei in this gap, mass 5 and mass 8, are completely unstable, the rest disintegrate in a very short time under stellar conditions. Reaction (31) however leads to stable C^{12} . This nucleus can now capture a further alpha particle



The temperatures required for this are about the same as for (31). There is also some capture of alpha particles by O^{16} leading to Ne^{20} , but the next step, $\text{Ne}^{23} \rightarrow \text{Mg}^{24}$, cannot occur appreciably at these temperatures; instead, the helium gets used up in forming C^{12} , O^{16} and some Ne^{20} .

Helium is depleted first in the center, and now the same process repeats which previously took place with hydrogen. A shell of burning He is formed, at a smaller radius than the H shell, and of course at a higher temperature. The center of the star now contracts further by gravitation and reaches still higher temperatures.

Buildup and dispersal of elements

The further developments of a massive star are more speculative. However the theory of Hoyle and collaborators¹⁸ is likely to be correct.

The center of the star heats up until the newly formed carbon nuclei can react with each other. This happens at a temperature of roughly 10^9 degrees. Nuclei like Mg^{24} or Si^{28} can be formed. There are also more complicated mechanisms in which we first have a capture reaction with emission of a gamma ray, followed by capture of this gamma ray in another nucleus which releases He^4 . This He^4 can then enter further nuclei and build up the entire chain of stable nuclei up to the most stable Fe. Not much energy is released in all of these processes.

The center of the star contracts further and gets still hotter. At very high temperatures, several milliards of degrees, thermal equilibrium is no longer strongly in favor of nuclei of the greatest binding energy. Instead, endothermic processes can take place which destroy some of the stable nuclei already formed. In the process, alpha particles, protons and even neutrons may be released. This permits the buildup of elements beyond Fe, up to the top of the periodic table. Because of the high temperatures involved all this probably goes fairly fast, perhaps in thousands of years.

During this stage, nuclear processes tend to consume rather than release energy. Therefore they no longer oppose the gravitational contraction so that contraction continues unchecked. It is believed that this will lead to an unstable situation. Just as the first contraction, at the formation of the H shell source, led to an expansion of the outer envelope of the star, a similar outward expansion is expected now. But time scales are now short, and this expansion may easily be an explosion. Hoyle, et al, have suggested this as the mechanism for a supernova.

In a supernova explosion much of the material of the star is ejected into interstellar space. We see this, eg,

in the Crab Nebula. The ejected material probably contains the heavy elements which have been formed in the interior of the massive star. Thus heavy elements get into the interstellar gas, and can then be collected again by newly forming stars. It is believed that this is the way how stars get their heavy elements. This means that most of the stars we see, including our sun, are at least second generation stars, which have collected the debris of earlier stars which have suffered a supernova explosion.

To clinch this argument it must be shown that heavy elements cannot be produced in other ways. This has indeed been shown by Fowler.¹⁹ He has investigated the behavior of the enormous gas cloud involved in the original "Big Bang," and its development with time. He has shown that temperatures and densities, as functions of time, are such that heavy elements beginning with C cannot be produced. The only element which can be produced in the big bang is He^4 .

If all this is true, stars have a life cycle much like animals. They get born, they grow, they go through a definite internal development, and finally they die, to give back the material of which they are made so that new stars may live.

* * *

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